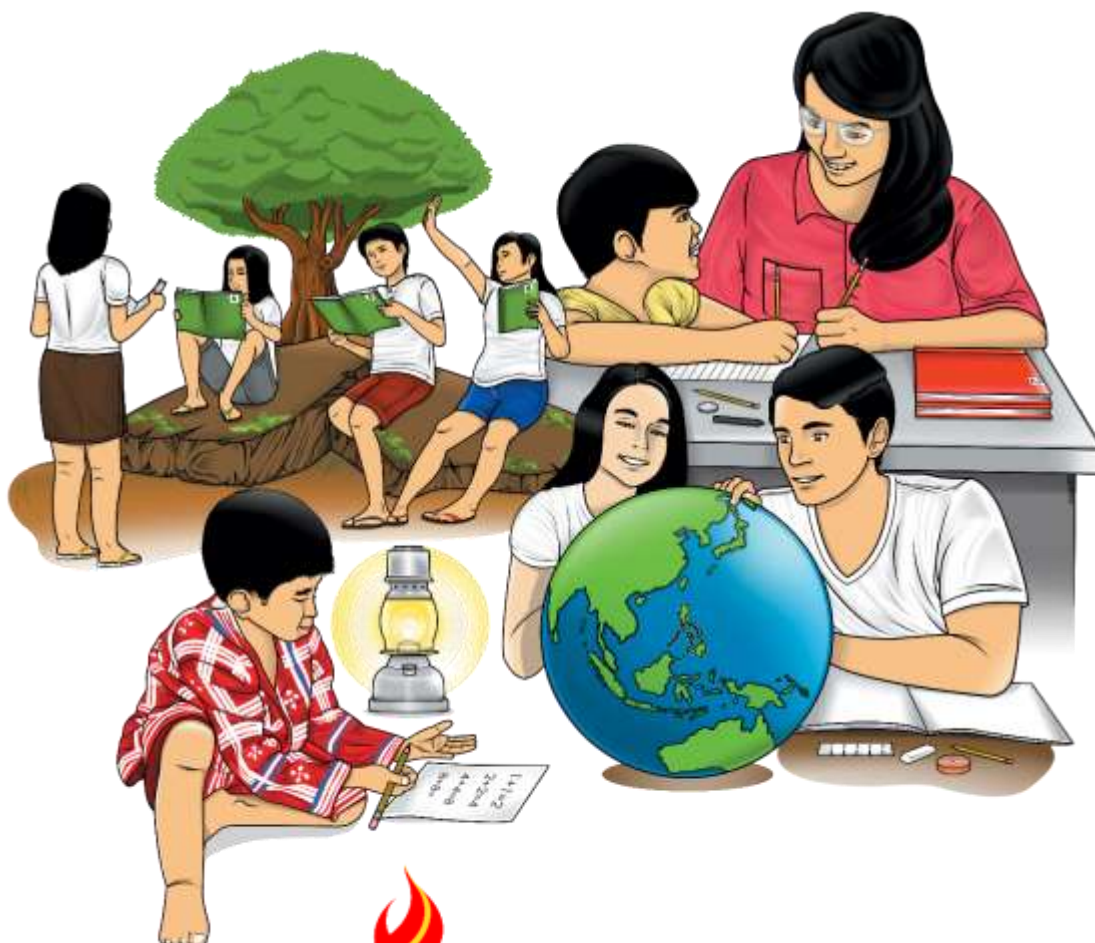


# Mathematics

## Quarter 1 – Module 5A: “Multiplying and Dividing Rational Algebraic Expressions”



**Mathematics – Grade 8**  
**Alternative Delivery Mode**  
**Quarter 1 – Module 5A: Multiplying and Dividing Rational Algebraic Expressions**  
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**Development Team of the Module**

<b>Writers:</b>	Jenny O. Pendica, Alicia E. Gonzales
<b>Language Editor:</b>	Merjorie G. Dalagan
<b>Content Evaluator:</b>	Alsie Mae M. Perolino
<b>Layout Evaluator:</b>	Jake D. Fraga
<b>Reviewers:</b>	Rhea J. Yparraguirre, Nilo B. Montaña, Lilibeth S. Apat, Liwayway J. Lubang, Rhodora C. Luga, Lee C. Apas, Jenny O. Pendica, Vincent Butch S. Embolode, Emmanuel S. Saga
<b>Layout Artist:</b>	Fritch A. Paronda
<b>Management Team:</b>	Francis Cesar B. Bringas, Isidro M. Biol, Jr., Maripaz F. Magno, Josephine Chonie M. Obseñares, Josita B. Carmen, Celsa A. Casa, Regina Euann A. Puerto, Bryan L. Arreo, Lieu Gee Keeshia C. Guillen, Claire Ann P. Gonzaga, Leopardo P. Cortes, Jr.

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**Department of Education – Caraga Region**

Office Address: Learning Resource Management Section (LRMS)  
J.P. Rosales Avenue, Butuan City, Philippines 8600  
Telefax No.: (085) 342-8207 / (085) 342-5969  
E-mail Address: caraga@deped.gov.ph

# **Mathematics**

## **Quarter 1 – Module 5A:**

### **“Multiplying and Dividing Rational Algebraic Expressions”**

## **Introductory Message**

This Self-Learning Module (SLM) is prepared so that you, our dear learners, can continue your studies and learn while at home. Activities, questions, directions, exercises, and discussions are carefully stated for you to understand each lesson.

Each SLM is composed of different parts. Each part shall guide you step-by-step as you discover and understand the lesson prepared for you.

Pre-tests are provided to measure your prior knowledge on lessons in each SLM. This will tell you if you need to proceed on completing this module or if you need to ask your facilitator or your teacher's assistance for better understanding of the lesson. At the end of each module, you need to answer the post-test to self-check your learning. Answer keys are provided for each activity and test. We trust that you will be honest in using these.

In addition to the material in the main text, Notes to the Teacher are also provided to our facilitators and parents for strategies and reminders on how they can best help you on your home-based learning.

Please use this module with care. Do not put unnecessary marks on any part of this SLM. Use a separate sheet of paper in answering the exercises and tests. And read the instructions carefully before performing each task.

If you have any questions in using this SLM or any difficulty in answering the tasks in this module, do not hesitate to consult your teacher or facilitator.

Thank you.





13. Below are the steps in finding the quotients of rational algebraic expressions. Which of the following is in correct order?

- I. Divide out common factors.
- II. Simplify the remaining factors.
- III. Find the reciprocal of the divisor and proceed to multiplication.
- IV. Determine the dividend and divisor of the given expression.

- A. I, II, III
- B. II, III, IV
- C. IV, III, I, II
- D. IV, I, II, III

14. Given the expression  $\frac{a^2+a}{3a-15} \div \frac{a^2+2a+1}{6a-30}$ , which of the following statements is true?

- A. The divisor is  $\frac{a^2+a}{3a-15}$ .
- B. The reciprocal of the divisor is  $\frac{3a-15}{a^2+a}$ .
- C. The common factors that can be divided out are  $(a+1)(3a-15)$ .
- D. The quotient obtained after dividing the expressions  $\frac{a^2+a}{3a-15} \div \frac{a^2+2a+1}{6a-30}$  is  $\frac{2a}{a+1}$ .

15. Your classmate multiplied rational algebraic expressions as presented below.

$$\frac{x+3}{2} \cdot \frac{2}{x+3} = \frac{x+3}{2} \cdot \frac{x+3}{2} = \frac{x^2+6x+9}{4}$$

Is your classmate's solution correct?

- A. Yes. There is a need to get the reciprocal of the second factor.
- B. Yes. The product obtained after multiplying the expressions is correct.
- C. No. Getting the reciprocal is not applicable in multiplying rational expressions.
- D. No. The product obtained after multiplying the rational algebraic expressions is wrong.

## Lesson

# 1

# Multiplying and Dividing Rational Algebraic Expressions

Whether you go by the boat, by car, or by plane, traveling can be a lot of fun. It is also very educational as it gives you firsthand experiences about things you just see on TV or read in the papers or in books.

But do you realize how much mathematical concepts can be involved in traveling? For example, do you know how far you can reach by a bus if it is traveling  $\frac{37}{2}$  km/h for  $\frac{1}{4}$  of an hour?



## What's In

Rational algebraic expressions are multiplied the same way as you would multiply regular fractions. So, let us recall multiplication of fractions.

Directions: Match the expressions in Column A with its product in Column B and answer the questions that follow. Use another paper for your answer.

Column A		Column B	
1.	$\frac{4}{3} \cdot \frac{5}{7}$	A.	$\frac{1}{6}$
2.	$\frac{2}{5} \cdot \frac{3}{2}$	B.	$\frac{20}{21}$
3.	$\frac{5}{10} \cdot \frac{2}{6}$	C.	$\frac{3}{5}$
4.	$\frac{3}{9} \cdot \frac{12}{15}$	D.	$\frac{9}{5}$
5.	$\frac{3}{5} \cdot 3$	E.	$\frac{4}{15}$
		F.	$\frac{3}{4}$

Questions:

1. Do the fractions in Item 1 of Column A have greatest common factor (GCF) other than 1?
2. Do the fractions in Items 2 to 4 in Column A have GCFs other than 1? How did you find them?
3. What did you do to the GCFs of Items 2 to 4 in Column A? Why?
4. Were you able to divide out a factor of one fraction paired with a factor of the other fraction? Was it allowed?
5. How do you multiply fractions?





## What's New

Situation: Corona Virus Disease 2019 (CoVID-19) affects almost everyone around the globe. Governments have employed various proactive measures to flatten the curve of its spread. All these measures head towards the aim of keeping everyone at home as much as possible. In effect, many have lost their jobs and food on the table become scarce. Driven by the spirit of helpfulness, your churchmates distribute relief goods to different places. Using the church's vehicle, they travel at a speed of  $30 \text{ km/hr}$ . How far will your churchmates reach after 25 minutes of travel? Suppose the distance (in  $\text{km}$ ) is represented by  $x$ , and the time (in  $\text{hours}$ ) is represented by  $y$ , how far will your churchmates reach if they travel  $\frac{y+1}{14} \text{ hours}$ ?  $\frac{y-5}{20} \text{ hours}$ ? Complete the table below and answer the questions that follow. The first one is done for illustration. Remember that  $\text{Speed} \cdot \text{Time} = \text{Distance}$ .

	Speed	Time	Distance
1	$30 \text{ km/hr}$	$25 \text{ minutes} = \frac{1}{4} \text{ hr.}$	$\frac{30}{4} \text{ km} = 7\frac{1}{2} \text{ km}$
2	$30 \text{ km/hr}$	$\frac{y+1}{14} \text{ hrs.}$	
3	$30 \text{ km/hr}$	$\frac{y-5}{20} \text{ hrs.}$	

Questions:

1. How did you solve for distance?
2. What did you do to the common factors in the numerator and denominator? Why?
3. What do you call each entry of Columns 2 and 3?
4. How do you multiply rational algebraic expressions?



## What is It

The concept of multiplying the numerators and the denominators of fractions also applies to multiplying rational algebraic expressions. For example, the distance in the previous activity is solved by multiplying the numerators and denominators of the speed and time of travel. In addition to just multiplying the numerators and denominators, there are methods of reducing the product into its lowest forms. Multiplying rational algebraic expressions and methods of reducing the product in lowest form will be discussed using series of examples.

The first two examples will be using monomials to illustrate multiplication of rational algebraic expressions.

**Method 1: Divide Out Greatest Common Monomial Factor (GCMF) After Multiplying**

Example 1:  $\frac{37x}{2y} \cdot \frac{y}{4}$

Solution:

Step 1. Multiply the numerators and denominators of the given rational algebraic expressions.

$$37x \cdot y = 37xy \quad \text{Multiply the numerators.}$$

$$2y \cdot 4 = 8y \quad \text{Multiply the denominators.}$$

Step 2: Find the GCMF of the product of numerators and denominators.

$$37xy = 37 \cdot x \cdot y \quad \text{Look for prime factors.}$$

$$8y = 2 \cdot 2 \cdot 2 \cdot y \quad \text{Look for prime factors.}$$

$$GCF = y \quad \text{Look for the common factors from the two groups of factors.}$$

Step 3: Divide out the GCMF of the product of numerators and denominators.

$$\begin{aligned} \frac{37x}{2y} \cdot \frac{y}{4} &= \frac{37xy}{8y} && \text{Product (not yet reduced)} \\ &= \frac{37x\cancel{y}}{8\cancel{y}} && \text{Divide out GCMF.} \end{aligned}$$

Step 4: Simplify the remaining factors.

$$\frac{37x}{2y} \cdot \frac{y}{4} = \frac{37x}{8} \quad \text{Product in reduced form.}$$

**Method 2: Divide Out Greatest Common Monomial Factor (GCMF) Before Multiplying**

Example 2:  $\frac{15y}{2y} \cdot \frac{2y}{5x^2}$

Solution:

Step 1. Find the GCMF of the of numerators and denominators

$$15y \cdot 2y = 3 \cdot 5 \cdot y \cdot 2 \cdot y \quad \text{Look for prime factors of the two numerators.}$$

$$2y \cdot 5x^2 = 2 \cdot y \cdot 5 \cdot x \cdot x \quad \text{Look for prime factors of the two denominators.}$$

$$GCF = 2 \cdot y \cdot 5 \quad \text{Look for common factors from the numerators and denominators.}$$

Step 2: Divide out the GCMF of the numerators and denominators.

$$\frac{15y}{2y} \cdot \frac{2y}{5x^2} = \frac{\cancel{3} \cdot \cancel{5} \cdot \cancel{y}}{\cancel{2} \cdot \cancel{y}} \cdot \frac{\cancel{2} \cdot y}{\cancel{5} \cdot x \cdot x} \quad \text{Factorization of the numerators and denominators.}$$

$$= \frac{3 \cdot 5 \cdot y}{2 \cdot y} \cdot \frac{2 \cdot y}{5 \cdot x \cdot x} \quad \text{Divide out GCMF.}$$

Step 3: Simplify the remaining factors.

$$\frac{15y}{2y} \cdot \frac{2y}{5x^2} = \frac{3}{1} \cdot \frac{y}{x \cdot x} \quad \text{Remaining factors}$$

$$= \frac{3}{1} \cdot \frac{y}{x \cdot x} \quad \text{Multiply the numerators. Multiply the denominators.}$$

$$= \frac{3y}{x^2} \quad \text{Product in reduced form.}$$

The methods illustrated by the previous examples can also be used to rational algebraic expressions involving polynomials.

### Method 1: Divide Out Greatest Common Monomial Factor (GCMF) After Multiplying

Example 1:  $\frac{x^2-4}{2} \cdot \frac{4}{x-2}$

Solution:

Step 1. Multiply the numerators and denominators of the given rational algebraic expressions.

$$(x^2 - 4)(4) = (x^2)(4) - (4)(4) \quad \text{Distributive Property}$$

$$= 4x^2 - 16 \quad \text{Simplified}$$

$$(2)(x - 2) = (2)(x) - (2)(2) \quad \text{Distributive Property}$$

$$= 2x - 4 \quad \text{Simplified}$$

Step 2: Find the GCMF of the product of numerators and denominators.

$$\begin{aligned}
 4x^2 - 16 &= (2x - 4)(2x + 4) && \text{Factoring Difference of Two Squares} \\
 &= (2)(x - 2)(2)(x + 2) && \text{Factoring the Greatest Common Monomial Factor (GCMF)} \\
 2x - 4 &= 2(x - 2) && \text{Factoring the Greatest Common Monomial Factor (GCMF)} \\
 \text{GCMF} &= 2(x - 2) && \text{Look for the common factors from the numerators and denominators.}
 \end{aligned}$$

Step 3: Divide out the GCMF of the product of numerators and denominators.

$$\begin{aligned}
 \frac{x^2 - 4}{2} \cdot \frac{4}{x - 2} &= \frac{4x^2 - 16}{2x - 4} && \text{Product (not yet reduced)} \\
 &= \frac{(2)(x - 2)(2)(x + 2)}{2(x - 2)} && \text{Factored form of the numerator and denominator.} \\
 &= \frac{\cancel{(2)}\cancel{(x - 2)}(2)(x + 2)}{\cancel{2}\cancel{(x - 2)}} && \text{Divide out the GCMF.}
 \end{aligned}$$

Step 4: Simplify the remaining factors.

$$\begin{aligned}
 \frac{x^2 - 4}{2} \cdot \frac{4}{x - 2} &= 2(x + 2) && \text{Remaining factors} \\
 &= (2)(x) + (2)(2) && \text{Distributive Property} \\
 &= 2x + 4 && \text{Product in reduced form.}
 \end{aligned}$$

### Method 2: Divide Out Greatest Common Monomial Factor (GCMF) Before Multiplying

Example 2:  $\frac{x-5}{x^2-7x+10} \cdot \frac{x^2+x-6}{5}$

Solution:

Step 1. Find the GCMF of the of numerators and denominators

$$\begin{aligned}(x-5)(x^2+x-6) &= (x-5)\underbrace{(x^2+x-6)} && \text{Factor the trinomial.} \\ &= (x-5)(x+3)(x-2) && \text{Retain the other factor and} \\ &&& \text{write the factors of the} \\ &&& \text{trinomial.}\end{aligned}$$

$$\begin{aligned}(x^2-7x+10)(5) &= \underbrace{(x^2-7x+10)}(5) && \text{Factor the trinomial.} \\ &= (x-5)(x-2)(5) && \text{Write the factors of the} \\ &&& \text{trinomial and retain the} \\ &&& \text{other factor.}\end{aligned}$$

$$GCF = (x-5)(x-2) \quad \text{Look for common factors from the numerators and denominators.}$$

Step 2: Divide out the GCMF of the numerators and denominators.

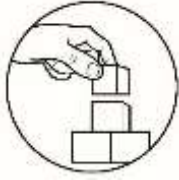
$$\begin{aligned}\frac{x-5}{x^2-7x+10} \cdot \frac{x^2+x-6}{5} &= \frac{(x-5)(x+3)(x-2)}{(x-5)(x-2)(5)} && \text{Factorization of the} \\ &&& \text{numerators and} \\ &&& \text{denominators.} \\ &= \frac{\cancel{(x-5)}(x+3)\cancel{(x-2)}}{\cancel{(x-5)}\cancel{(x-2)}(5)} && \text{Divide out GCMF.}\end{aligned}$$

Step 3: Simplify the remaining factors.

$$\frac{x^2+x-6}{5} \cdot \frac{x-5}{x^2-7x+10} = \frac{x+3}{5} \quad \text{Product in reduced form.}$$

### DON'T FORGET

In multiplying rational algebraic expressions, either before or after multiplying, always divide out the common factors to attain the product in reduced form.



## What's More

A. Find the product of the following rational algebraic expressions by **dividing out the GCMF after multiplying**. Use another paper for your answers.

1.  $\frac{3x}{4} \cdot \frac{8}{9}$

2.  $\frac{2x-2}{3} \cdot \frac{2}{x^2-1}$

Questions:

1. What was the first step that you did to find the products of the problems given?
2. What did you do to the GCMFs that you found in each of the items? Why?
3. What did you do last?

B. Find the product of the following rational algebraic expressions by **dividing out the GCMF before multiplying**.

1.  $\frac{7}{2x^3} \cdot \frac{x^2}{21}$

2.  $\frac{x+2}{x^2-14x+49} \cdot \frac{x-7}{2}$

Questions:

1. What was the first step that you did to find the products of the problems given?
2. What did you do to the GCMFs that you found in each of the items? Why?
3. What did you do last?

C. Find the product. You may use any of the discussed methods to perform the operation.

1.  $\frac{7}{x^2-4} \cdot \frac{x(x-2)}{14}$

Questions:

1. What method did you use?
2. What made you decide whether to use Method 1 or Method 2?



## What I Have Learned

Situation: Your classmate asks for help to complete the solution-explanation card of the problem below. Please do help!

$$(3y) \cdot \frac{y^2 + 3y - 4}{y^2 + 5y + 4}$$

Solution

$$\begin{aligned}
(3y) \cdot \frac{y^2 + 3y - 4}{y^2 + 5y + 4} &= (\underline{\quad}) \cdot \frac{(y + 4)(\underline{\quad})}{(y + 1)(\underline{\quad})} \\
&= (\underline{\quad}) \cdot \frac{(y + 4)(\underline{\quad})}{(y + 1)(\underline{\quad})} \\
&= (\underline{\quad})(\underline{\quad}) \\
&= \underline{\hspace{2cm}}
\end{aligned}$$

Explanation

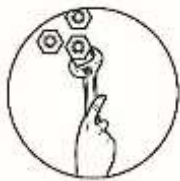
I know how to \_\_\_\_\_.

First, \_\_\_\_\_.

After that, \_\_\_\_\_.

Then, \_\_\_\_\_.

Finally, \_\_\_\_\_.



## What I Can Do

Situation: Your friend is planting sweet potato on a rectangular plot. Suppose the number of sweet potatoes planted is represented by  $x$  and the length of the plot is  $\frac{x-3}{4}$  units while the width is  $\frac{2x}{x+3}$  units.

Questions:

1. What shall your friend do to find the area of the rectangular plot?
2. What is the area of the rectangular plot? Show your solution.

**Lesson**

**2**

# Dividing Rational Algebraic Expressions

The previous lesson made you understand that multiplying rational algebraic expressions is the same with multiplying fractions. Do you think dividing rational algebraic expressions is also the same with dividing fractions?



## What's In

Recall dividing fractions. Match the expression in Column A with its quotient in Column B. Write your answers on another sheet of paper.

Column A		Column B	
1.	$\frac{4}{3} \div \frac{5}{7}$	A.	$\frac{3}{5}$
2.	$\frac{2}{5} \div \frac{2}{3}$	B.	2
3.	$6 \div \frac{6}{2}$	C.	$\frac{3}{28}$
4.	$\frac{3}{7} \div 4$	D.	1
5.	$\frac{3}{5} \div \frac{3}{5}$	E.	$\frac{4}{15}$
		F.	$\frac{28}{15}$

Questions:

1. In each item in Column A, which of the expression is the divisor – is it the first or the second fraction?
2. What did you do to the divisors to find the quotients?
3. What operation did you use to replace the division operation?
4. What did you do to the Greatest Common Factor (GCF) of Items 2, 3, and 5? Why did you do so?
5. How do you divide fractions?



## What's New

Ellen, a Grade 8 student, was assigned to solve the problem:  $\frac{x^2-9}{x-3} \div \frac{x+3}{x-3}$ . To solve this, she performed the following steps:



Step 1. Applying her knowledge in dividing fractions, she rewrote the problem as

$$\frac{x^2 - 9}{x - 3} \cdot \frac{x - 3}{x + 3}$$

Step 2. Multiply.

$$\frac{x^2 - 9}{x - 3} \cdot \frac{x - 3}{x + 3} = \frac{x^3 - 9x - 3x^2 + 27}{x^2 - 6x + 9}$$

Step 3. Ellen concluded that  $\frac{x^3 - 9x - 3x^2 + 27}{x^2 - 6x + 9}$  is the quotient of the given rational algebraic expressions in its simplest form.

Questions:

1. Is Ellen's answer correct? Elaborate your answer.
2. What did Ellen do in Step 1?
3. What suggestions could you make to help Ellen in Step 2?
4. What is the quotient of the given rational algebraic expressions?
5. How would you divide the rational algebraic expressions?



## What is It

The quotient of two rational algebraic expressions is the product of the dividend and the reciprocal of the divisor. In symbols,

$$\frac{a}{b} \div \frac{c}{d} = \frac{a}{b} \cdot \frac{d}{c} = \frac{ad}{bc}, b, c, d \neq 0$$

To help you understand how to divide rational algebraic expressions, examine the examples in the next page.

Example 1:  $\frac{x+y}{x-y} \div \frac{x}{y}$

Solution:

Step 1. Determine the dividend and divisor of the expression.

$$\begin{array}{ccc} \frac{x+y}{x-y} & \div & \frac{x}{y} \\ \downarrow & & \downarrow \\ \text{Dividend} & & \text{Divisor} \end{array}$$

Step 2: Find the reciprocal of the divisor.

$$\frac{x}{y} \rightarrow \frac{y}{x}$$

Reciprocal means its multiplicative inverse.

Step 3: Multiply the dividend with the reciprocal of the divisor.

$$\begin{aligned} \frac{x+y}{x-y} \div \frac{x}{y} &= \frac{(x+y) \cdot y}{(x-y) \cdot x} && \text{Multiply numerator with numerator.} \\ &= \frac{(x+y) \cdot y}{(x-y) \cdot x} && \text{Multiply denominator with denominator.} \\ &= \frac{(x)(y) + (y)(y)}{(x)(x) - (y)(x)} && \text{Distributive Property} \\ &= \frac{xy + y^2}{x^2 - xy} && \text{Quotient in reduced form} \end{aligned}$$

Example 2:  $\frac{3p^2+6p+3}{p+1} \div \frac{3}{p}$

Solution:

Step 1. Determine the dividend and divisor of the expression.

$$\begin{array}{ccc} \frac{3p^2 + 6p + 3}{p + 1} & \div & \frac{3}{p} \\ \downarrow & & \downarrow \\ \text{Dividend} & & \text{Divisor} \end{array}$$

Step 2: Find the reciprocal of the divisor.

$$\frac{3}{p} \rightarrow \frac{p}{3} \quad \text{Reciprocal of the divisor is its multiplicative inverse.}$$

Step 3: Multiply the dividend with the reciprocal of the divisor.

$$\begin{aligned} \frac{3p^2 + 6p + 3}{p + 1} \div \frac{3}{p} &= \frac{3p^2 + 6p + 3}{p + 1} \cdot \frac{p}{3} && \text{Dividend times the reciprocal of divisor.} \\ &= \frac{(3p + 3)(p + 1)}{(p + 1)} \cdot \frac{(p)}{(3)} && \text{Factoring Trinomial (numerator 1)} \\ &= \frac{(3)(p + 1)(p + 1)}{(p + 1)} \cdot \frac{(p)}{(3)} && \text{Factoring the GCMF (numerator 1)} \\ &= \frac{\cancel{(3)}(p + 1)\cancel{(p + 1)}}{\cancel{(p + 1)}} \cdot \frac{(p)}{\cancel{(3)}} && \text{Divide out GCMF.} \end{aligned}$$

$$\begin{aligned}
 &= (p+1)p && \text{Simplify the remaining factors.} \\
 &= (p)(p) + (1)(p) && \text{Distributive Property} \\
 &= p^2 + 1 && \text{Quotient in reduced form}
 \end{aligned}$$

Example 3:  $\frac{x^2+5x+6}{x^2+4x+4} \div \frac{x+1}{x+3}$

Solution:

Step 1. Determine the dividend and divisor of the expression.

$$\begin{array}{ccc}
 \frac{x^2 + 5x + 6}{x^2 + 4x + 4} & \div & \frac{x + 1}{x + 3} \\
 \downarrow & & \downarrow \\
 \text{Dividend} & & \text{Divisor}
 \end{array}$$

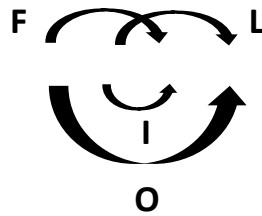
Step 2: Find the reciprocal of the divisor.

$$\frac{x + 1}{x + 3} \rightarrow \frac{x + 3}{x + 1}$$

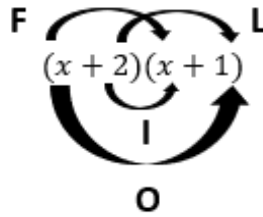
Reciprocal of the divisor is its multiplicative inverse.

Step 3: Multiply the dividend with the reciprocal of the divisor.

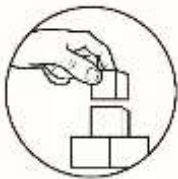
$$\begin{aligned}
 \frac{x^2 + 5x + 6}{x^2 + 4x + 4} \div \frac{x + 1}{x + 3} &= \frac{x^2 + 5x + 6}{x^2 + 4x + 4} \cdot \frac{x + 3}{x + 1} && \text{Dividend times the reciprocal of the divisor.} \\
 &= \frac{(x + 2)(x + 3)}{(x + 2)(x + 2)} \cdot \frac{(x + 3)}{(x + 1)} && \text{Factoring Trinomial (numerator 1 and denominator 1)} \\
 &= \frac{\cancel{(x + 2)}(x + 3)}{\cancel{(x + 2)}(x + 2)} \cdot \frac{(x + 3)}{(x + 1)} && \text{Divide out GCMF.} \\
 &= \frac{(x + 3)(x + 3)}{(x + 2)(x + 1)} && \text{Use FOIL to simplify the remaining factors. (See process below.)} \\
 &= \frac{x^2 + 6x + 9}{x^2 + 3x + 2} && \text{Quotient} \\
 &= (x + 3)(x + 3)
 \end{aligned}$$



Terms Multiplied	Expression	Product	Final Product
<b>F</b> irst Terms	$(x)(x)$	$= x^2$	$= x^2$
<b>O</b> uter Terms	$(x)(3)$	$= 3x$	$= 6x$
<b>I</b> nner Terms	$(3)(x)$	$= 3x$	$= 9$
<b>L</b> ast Terms	$(3)(3)$	$= 9$	$= x^2 + 6x + 9$



Terms Multiplied	Expression	Product	Final Product
<b>F</b> irst Terms	$(x)(x)$	$= x^2$	$= x^2$
<b>O</b> uter Terms	$(x)(1)$	$= x$	$= 3x$
<b>I</b> nner Terms	$(2)(x)$	$= 2x$	$= 2$
<b>L</b> ast Terms	$(2)(1)$	$= 2$	$= x^2 + 3x + 2$



## What's More

Divide the following rational algebraic expressions and answer the questions that follow.

A.  $\frac{a-b}{a+b} \div \frac{b}{a}$

B.  $\frac{2x^2+4x+2}{x+1} \div \frac{2}{x}$

Questions:

1. What are the divisors in each expression? What did you do to the divisors to get the quotient?
2. What factoring techniques did you use to find the GCMF? What did you do to the GCMFs?
3. How did you simplify the quotient?

C.  $\frac{x^2+6x+9}{x^2+3x+2} \div \frac{x+3}{x-1}$

Questions:

1. From the expression, which is the divisor? What did you do to the divisor to find the quotient?
2. What factoring techniques did you use to find the GCMF? What did you do to the GCMFs?

3. How did you simplify the resulting expression?



## What I Have Learned

Situation: You take the lead in explaining to your group the solution of the problem below. Complete your explanation below. You may choose words, terms, or phrases from the box.

$$\frac{x^2 - 5x + 6}{y^2} \div \frac{x - 2}{y}$$

As you all know, the problem is telling us to \_\_\_\_\_. To begin solving this, we have to \_\_\_\_\_. You have to remember that the \_\_\_\_\_ is the expression that follows after the \_\_\_\_\_. So now, because the divisor is \_\_\_\_\_, its reciprocal is \_\_\_\_\_. Then, we need to factor our numerators and \_\_\_\_\_. By Factoring Trinomial,  $x^2 - 5x + 6 = (\text{_____})(\text{_____})$ . After factoring we have to change the operation to be used, from division it will become \_\_\_\_\_. Then, we have to \_\_\_\_\_ common factors to ensure that our quotient will be in \_\_\_\_\_. So, the common factors to be divided out are \_\_\_\_\_. Finally, the simplified remaining factors \_\_\_\_\_ is our quotient.

determine the divisor	divisor	multiplication	$(x - 2)$	denominator
divide out	$\frac{x - 3}{y}$	division sign	$\frac{x - 2}{y}$	$y$
reduced form	divide rational algebraic expressions		$(x - 3)(x - 2)$	$\frac{y}{x - 2}$



## What I Can Do

Read the situation below and answer the questions that follow.

Your school organized a tree planting activity participated by all learners and teachers in Grades 7 to 10. To protect the newly planted trees from the harsh environment, a triangular tree guard was installed. The base ( $b$ ) of one side of the

triangular tree guard in terms of  $x$  is  $\frac{2x^2+4x+2}{x-1}$  units and its area ( $A$ ) is  $x^2 + 5x + 4$  square units.

Questions:

1. What is the height ( $h$ ) of the triangular tree guard in terms of  $x$ ? (Recall that  $A = \frac{1}{2}bh$ ).
2. What did you do to find the height of the triangular tree guard?



## Assessment

Choose the correct answer. Write your answers on a separate sheet of paper.

1. What is the reduced form of  $\frac{4}{2ab^2} \cdot \frac{ab}{4}$ ?
 

A. $\frac{1}{5b}$	C. $\frac{1}{3b}$
B. $\frac{1}{4b}$	D. $\frac{1}{2b}$
2. What are the common factors in the numerators and denominators of  $\frac{2a}{bc} \cdot \frac{abc}{a}$ ?
 

A. $abc$	C. $a^2bc$
B. $a^2bc$	D. $abc^2$
3. Find the product of  $\frac{7}{8-2a} \cdot \frac{4-a}{2}$ .
 

A. $\frac{5}{4}$	C. $\frac{7}{4}$
B. $\frac{6}{4}$	D. $\frac{8}{4}$
4. What is the simplest form of  $\frac{2}{x^2+x} \cdot \frac{3x+3}{x}$ ?
 

A. $\frac{6}{x^5}$	C. $\frac{6}{x^3}$
B. $\frac{6}{x^4}$	D. $\frac{6}{x^2}$
5. What are the common factors in the numerators and denominators of  $\frac{x^2-9}{x^2+x-20} \cdot \frac{x^2-8x+16}{3x-9}$ ?
 

A. $x + 3$	C. $(x + 3)(x - 4)$
B. $x - 4$	D. $(x - 3)(x - 4)$
6. Find the product of  $\frac{x^2-9}{x^2+x-20} \cdot \frac{x^2-8x+16}{3x-9}$ .
 

A. $\frac{x^2-x-10}{3x+12}$	C. $\frac{x^2-x-14}{3x+18}$
B. $\frac{x^2-x-12}{3x+15}$	D. $\frac{x^2-x-16}{3x+21}$



15. Your classmate divided rational algebraic expressions as presented below.

$$\frac{x+3}{2} \div \frac{2}{x+3} = \frac{\cancel{x+3}}{\cancel{2}} \div \frac{\cancel{2}}{\cancel{x+3}} = 1$$

Is your classmate's solution correct?

- A. Yes. The solution presented is correct.
- B. Yes. Common factors can be directly divided out.
- C. No. The correct answer should be equal to  $\frac{4}{(x+3)^2}$ .
- D. No. Get the reciprocal of the divisor first, then multiply.



## ***Additional Activities***

Write a poem about multiplying and dividing rational algebraic expressions. You may include your experience in going through the activities in this lesson. Use a separate sheet of paper. The following will be the rubric for rating your output.

Categories and Criteria	Beginning (2)	Developing (3)	Accomplished (4)	Exemplary (5)
Content	Demonstrate 0 – 5 correct ideas about the lesson.	Demonstrate 6 -7 correct ideas about the lesson.	Demonstrate 8 -9 correct ideas about the lesson.	Demonstrate 10 or more correct ideas about the lesson.
Conventions	The poem has 51% or more errors in spelling and grammar.	The poem has 31% - 50% errors in spelling and grammar.	The poem has 11% -30% errors in spelling and grammar.	No errors in spelling and grammar.
Originality	The poem is 51% - 100 % copied from another source.	The poem 31% - 50% copied from another source.	The poem is 11% -30% copied from another source.	The poem is 0%-10% copied.





# Answer Key

## Lesson 1

### What I Know

1. A

2. D

3. A

4. E

5. D

Questions:

1. None

2. Yes; By factorizing

3. Divide out common factors; To reduce the product into lowest form.

4. Yes; Yes

5. Multiply numerator with numerator and denominator with denominator, divide out common factors, simplify remaining factors.

10. A

11. B

12. C

13. C

14. D

15. C

1. A

2. D

3. A

4. E

5. D

Questions:

1. None

2. Yes; By factorizing

3. Divide out common factors; To reduce the product into lowest form.

4. Yes; Yes

5. Multiply numerator with numerator and denominator with denominator, divide out common factors, simplify remaining factors.

A.

1.  $\frac{2x}{3}$

2.  $\frac{3x+3}{4}$

Questions:

1. Multiply numerator with numerator and denominator with denominator.

2. Divide out; To reduce the product in lowest form.

3. Simplify the remaining factors.

B.

1.  $\frac{6x}{1}$

2.  $\frac{x+2}{2x-14}$

Questions:

1. Factorize the numerators and denominators.

2. Divide out; To reduce the product in lowest form.

3. Simplify the remaining factors.

C.

1.  $\frac{2x+4}{x}$

2. Divide out; To reduce the product in lowest form.

3. Simplify the remaining factors.

### What I Have Learned

Solution

$$(3y) \cdot \frac{y^2 + 3y - 4}{(y+4)(y-1)} = \frac{y^2 + 5y + 4}{(y+4)(y-1)} \cdot (3y) = \frac{(y+4)(y+1)}{(y+4)(y-1)} \cdot (3y) = \frac{(y+1)}{(y-1)} \cdot (3y) = \frac{3y^2 - 3y}{y+1} = \frac{y+1}{y+1}$$

### What's New

2.  $\frac{7}{15(y+1)} km$

3.  $\frac{2}{3(y-5)} km$

Questions:

1. Multiply speed with time.

2. Divide out; To reduce the product in lowest form.

3. Rational algebraic expressions

4. Multiply numerator with numerator and denominator with denominator, divide out common factor/s, simplify remaining factors.

### What I Can Do

Questions:

1. Multiply the length and width.

2.  $A = lw; \frac{4}{x-3} \cdot \frac{x+3}{2x} = \frac{2x+6}{x^2-3x}$  square units

**Lesson 2**

**What's In**

1. F

2. A

3. B

4. C

5. D

Questions:

1. Second

2. The multiplicative inverse or reciprocal

of each is determined.

3. Yes; Division; Multiplication

4. Divide out; To reduce the quotient into

lowest form.

5. Identify the dividend and divisor;

determine the reciprocal of the divisor,

factorize the numerators and denominators,

divide out common factors, simplify the

remaining factors.

**What's More**

A.  $\frac{a-b}{a-b} \div \frac{a}{b} = \frac{ab+b^2}{a^2-ab}$

B.  $\frac{x^2+4x+2}{2} \div \frac{x+1}{2} = x^2 + x$

Questions:

1.  $A = \frac{a}{b}$ ;  $B = \frac{x}{2}$ ; Find the reciprocal

2. Factoring GCMF and Factoring Trinomial

3. Apply distributive property

C.  $\frac{x^2+6x+9}{x^2+3x+2} \div \frac{x-1}{x^2+3x+2}$

Questions:

1.  $\frac{x-1}{x+3}$ ; Find the reciprocal

2. Factoring Trinomial; Divide out

3. Apply distributive property/ Multiply though FOIL Method.

**What I Have Learned**

As you all know the problem is telling us to **divide rational algebraic expressions**. To begin solving this, we have to **determine the divisor**. You have to remember that the **divisor** is the expression that follows after the **division sign**. So now, because the divisor is  $\frac{x}{x-2}$ , its reciprocal is  $\frac{x-2}{x}$ . Then, we need to factor our numerators and **denominator**. By Factoring Trinomial,  $x^2 - 5x + 6 = (x - 3)(x - 2)$ . After factoring we have to change the operation to be used, from division it will become **multiplication**. Then, we have to **divide out** common factors to ensure that our quotient will be in **reduced form**. So, the common factors to be divided out are  $(x - 2)$  and  $y$ . Finally, the simplified remaining factors  $\frac{y}{x-3}$  is our quotient.

**What's New**

Questions:

1. No.  $x^2 - 9$  is factorable as  $(x + 3)(x - 3)$ .

2. Get the reciprocal of the divisor and change

the operation to division.

3. Factor out  $x^2 - 9$  first, divide out common

factors before multiplying the remaining factors.

4.  $(x + 3)$

5. Identify the dividend and divisor; determine

the reciprocal of the divisor, factorize the

numerators and denominators, divide out

common factors, simplify the remaining factors.

**Assessment**

1. D

2. A

3. C

4. D

5. D

6. B

7. A

8. B

9. A

10. A

11. D

12. D

13. D

14. D

15. D

**What I Can Do**

1.  $A = \frac{1}{2}bh \rightarrow h = \frac{b}{2A} \rightarrow h = \frac{b}{2(2x^2 + 5x + 4)} \div \frac{x-1}{2x^2+4x+2}$

$\rightarrow 2(x^2 + 5x + 4) \cdot \frac{x-1}{2x^2+4x+2} \rightarrow \frac{2x^2+4x+2}{2(x^2+5x+4)(x-1)}$

$\rightarrow \frac{2(x^2 + 4)(x + 1)(x - 1)}{2(x^2 + 2x + 1)}$

$\rightarrow \frac{2(x + 4)(x + 1)(x - 1)}{2(x + 1)(x + 1)}$

$\rightarrow \frac{x + 1}{x^2 + 3x - 4}$

Hence, the height of the triangular tree guard is  $\frac{x+1}{x^2+3x-4}$  units.

2. By deriving the formula for finding the height of the triangle, substitute values and perform

operations on rational algebraic expressions.

## ***References***

Abuzo, E.P., Bryant, M.L., Cabrella, J.B., Caldez, B.P., Callanta, M.M., Castro, A.I., Halabaso, A.R., et. al (2013). Mathematics 8 - Learner's Module. Department of Education, Pasig City, Philippines, pp. 81-104

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**For inquiries or feedback, please write or call:**

Department of Education - Bureau of Learning Resources (DepEd-BLR)

Ground Floor, Bonifacio Bldg., DepEd Complex  
Meralco Avenue, Pasig City, Philippines 1600

Telefax: (632) 8634-1072; 8634-1054; 8631-4985

Email Address: [blr.lrqad@deped.gov.ph](mailto:blr.lrqad@deped.gov.ph) \* [blr.lrpd@deped.gov.ph](mailto:blr.lrpd@deped.gov.ph)